1) 

a)

| 12 | 15 |
| :---: | :---: |
| $1,12,2,6$, <br> 3,4 | $1,15,3,5$ |
| 1,3 |  |

b)

| 24 | 36 |
| :---: | :--- |
| $1,24,2,12$, | $1,36,2,18$, |
| $3,8,4,6$ | $3,12,4$, <br> 9,6 |
| $1,2,3,4,6$ |  |

c)

| 81 | 60 |
| ---: | :---: |
| $1,81,3$, | $1,60,2,30,3,20$ |
| 27,9 | $4,15,5,12,6,10$ |
|  |  |
|  | 1,3 |

d)

| 45 | 16 |
| :---: | :--- |
| $1,45,3,15$, | $1,16,2$, |
| 5,9 | 8,4 |
|  |  |
| 1 |  |

e)

| 56 | 20 |
| :--- | :--- |
| $1,56,2$, | $1,20,2,10$, |
| $28,4,14$, | 4,5 |
| 7,8 |  |, | $1,2,4$ |
| :--- |

f)

| 28 | 48 |
| :--- | :--- |
| $1,28,2,14$, <br> 4,7 | $1,48,2,24,3,16$, <br> $4,12,6,8$ |
| $1,2,4$ |  |

2) Multiple answers possible. Here are some possibilities:
a)

| 3 |
| :--- |
| 12 and 15 or 81 and 60 or 36 |
| and 15 |

b)

| 4 |
| :--- |
| 56 and 20 or 28 and 48 or |
| 20 and 28 |

c)

| 6 |
| :--- |
| 24 and 36 or 12 and 18 or 6 |
| and 60 |

a) This is sometimes true. For example, 24 has 8 factors: 1 and $24 ; 2$ and $12 ; 3$ and $8 ;$ and 4 and 6 . So 24 has an even number of factors. However, 16 has 5 factors; 1 and 16; 2 and 8; and 4 .
b) This is sometimes true. For example, 45 and 15 are a pair of odd numbers. They have three common factors: 1, 3 and 5. 28 and 48 are a pair of even numbers. They also have three common factors: 1, 2 and 4. This proves that pairs of even numbers don't always have more common factors than odd numbers.
c) This is always true. Every number has at least two factors: I and itself. For example, 7 has two factors: 1 and 7.
d) This is never true. As every number has at least one pair of factors, I and itself, then every pair of numbers will always share at least one common factor: I. For example, 45 and 16 share only one common factor: I.

1) Aaron is correct. 8 is a common factor of 64 and 48.6 is only a factor of 48 , and not 64 .
2) 

a) He could cut the ribbon into lengths of $5 \mathrm{~cm}, 10 \mathrm{~cm}, 20 \mathrm{~cm}, 30 \mathrm{~cm}$ or 60 cm .
b) 40 is a factor of 240 , but it is not a factor of 180 . If he cut the 180 cm ribbon into 40 cm lengths, he would have 20 cm left over.

